

PART – B

(5 x 16 = 80 Marks)

Q.No.	Questions	Marks	KL	CO														
11. a)	i. Solve the following system of equations by Gauss seidel method $27x + 6y - z = 85,$ $x + y + 54z = 110,$ $6x + 15y + 2z = 72.$	8	K3	CO1														
	ii. Solve the system of equations by Gauss elimination method $x + 2y + z = 3,$ $2x + 3y + 3z = 10,$ $3x - y + 2z = 13.$	8	K3	CO1														
(OR)																		
b) i.	Find the largest eigenvalue and corresponding eigenvector of $\begin{pmatrix} 1 & 6 & 1 \\ 1 & 2 & 0 \\ 0 & 0 & 3 \end{pmatrix}$, by using power method.	8	K3	CO1														
	ii. Find the root of $x^3 - 2x - 5 = 0$ by the fixed point iteration method, correct to four decimal places.	8	K3	CO1														
12. a)	i. Using Newton's divided difference formula, find $f(x)$ from the following data and hence find $f(4)$.	8	K2	CO2														
	<table border="1" style="margin-left: 40px;"> <tr> <td>x:</td> <td>0</td> <td>1</td> <td>2</td> <td>5</td> </tr> <tr> <td>f(x):</td> <td>2</td> <td>3</td> <td>12</td> <td>147</td> </tr> </table>	x:	0	1	2	5	f(x):	2	3	12	147							
x:	0	1	2	5														
f(x):	2	3	12	147														
	ii. From the following data, find y at $x = 43$ using Newton's interpolation formula.	8	K2	CO2														
	<table border="1" style="margin-left: 40px;"> <tr> <td>x</td> <td>40</td> <td>50</td> <td>60</td> <td>70</td> <td>80</td> <td>90</td> </tr> <tr> <td>y</td> <td>184</td> <td>204</td> <td>226</td> <td>250</td> <td>276</td> <td>304</td> </tr> </table>	x	40	50	60	70	80	90	y	184	204	226	250	276	304			
x	40	50	60	70	80	90												
y	184	204	226	250	276	304												
(OR)																		
b)	The following values of x and y are given:	16	K4	CO2														
	<table border="1" style="margin-left: 40px;"> <tr> <td>x:</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> </tr> <tr> <td>y:</td> <td>1</td> <td>2</td> <td>5</td> <td>11</td> </tr> </table>	x:	1	2	3	4	y:	1	2	5	11							
x:	1	2	3	4														
y:	1	2	5	11														
	Find the cubic splines and evaluate $y(1.5)$.																	
13. a)	i. Use Gaussian three –point formula to evaluate $\int_1^5 \frac{dz}{z}$ and compare with exact value.	8	K3	CO3														
	ii. Using Romberg's integration to evaluate $I = \int_0^1 \frac{dx}{1+x}$ correct to four decimal places by taking $h = 0.5, 0.25$ & 0.125 .	8	K3	CO3														
(OR)																		

- b) i. Evaluate $\int_0^1 \int_0^1 \frac{1}{(1+x+y)} dx dy$ by Simpson's rule with $h = k = 0.5$. 8 K4 CO3

- ii. The following data gives the velocity of a particle for 20 seconds at different time intervals of duration 5 seconds. Find the initial acceleration using the entire data 8 K4 CO3

Time(sec.)	0	5	10	15	20
Velocity (m/sec.)	0	3	14	69	228

14. a) Given $\frac{dy}{dx} = 1 - y$ and $y(0)=0$, find 16 K4 CO4

- i. $y(0.1)$ by Taylor series method.
 ii. $y(0.2)$ and $y(0.3)$ by Euler's method.
 iii. $y(0.4)$ by Milne's method.

(OR)

- b) i. Using Runge-Kutta method of 4th order, solve $\frac{dy}{dx} = \frac{y^2 - x^2}{y^2 + x^2}$ with $y(0) = 1$ at $x = 0.2$. 8 K4 CO4

- ii. Using Taylor series method find y at $x = 0.1$ if $\frac{dy}{dx} = x^2 y - 1, y(0) = 1$ 8 K4 CO4

15. a) Solve the Poisson equation $\nabla^2 u = -10(x^2 + y^2 + 10)$ over the square with sides $x=0, y=0, x=3, y=3$ with $u=0$ on the boundary, taking $h=1$. 16 K5 CO5

(OR)

- b) Find the numerical solution of the parabolic equation $\frac{\partial^2 u}{\partial x^2} = 2 \frac{\partial u}{\partial t}$ when $u(0,t) = 0 = u(4,t)$ and $u(x,0) = x(4-x)$ by taking $h = 1$. Find the values upto $t = 5$. 16 K5 CO5